

1 / 8

$$1. (1 + 11 + 21 + 31 + 41) + (9 + 19 + 29 + 39 + 49) =$$

- A) 150 B) 199 C) 200 D) 249 E) 250

1989 Q1

1. E The sum is $5(50) = 250$ as can be seen by grouping the sum as shown.

$$(1 + 11 + 21 + 31 + 41) + (9 + 19 + 29 + 39 + 49)$$

OR

The sum is $10 + 30 + 50 + 70 + 90 = 250$ as can be seen by grouping the sum as shown.

$$(1 + 11 + 21 + 31 + 41) + (9 + 19 + 29 + 39 + 49)$$

2 / 8

$$1. \frac{10 - 9 + 8 - 7 + 6 - 5 + 4 - 3 + 2 - 1}{1 - 2 + 3 - 4 + 5 - 6 + 7 - 8 + 9} =$$

- (A) -1 (B) 1 (C) 5 (D) 9 (E) 10

1992 Q1

1. (B) Group the numerator in pairs from the left, and group the denominator in pairs from the left:

$$\frac{\overbrace{10-9}^1 + \overbrace{8-7}^1 + \overbrace{6-5}^1 + \overbrace{4-3}^1 + \overbrace{2-1}^1}{\underbrace{1-2}_{-1} + \underbrace{3-4}_{-1} + \underbrace{5-6}_{-1} + \underbrace{7-8}_{-1} + 9}$$

Hence, the answer is $\frac{5(1)}{4(-1) + 9} = \frac{5}{5} = 1$.

OR

Regroup the numerator and denominator into positive and negative terms,

$$\frac{(10 + 8 + 6 + 4 + 2) - (9 + 7 + 5 + 3 + 1)}{(1 + 3 + 5 + 7 + 9) - (2 + 4 + 6 + 8)} = \frac{30 - 25}{25 - 20} = \frac{5}{5} = 1.$$

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1985 Q2

2. $90 + 91 + 92 + 93 + 94 + 95 + 96 + 97 + 98 + 99 =$
 A) 845 B) 945 C) 1005 D) 1025 E) 1045

2. (B) By estimating, we see that the desired sum is between $10 \times 90 = 900$ and $10 \times 100 = 1000$, so it must be 945.

OR

Pair the numbers as shown. The sum of each pair is 189, so the desired sum is $5 \times 189 = 945$.

$$90 + 91 + 92 + 93 + 94 + 95 + 96 + 97 + 98 + 99$$

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1994 Q2

2. $\frac{1}{10} + \frac{2}{10} + \frac{3}{10} + \frac{4}{10} + \frac{5}{10} + \frac{6}{10} + \frac{7}{10} + \frac{8}{10} + \frac{9}{10} + \frac{55}{10} =$

(A) $4\frac{1}{2}$ (B) 6.4 (C) 9 (D) 10 (E) 11

2. (D) The sum of all the numerators is 100. Consequently, the sum of all the fractions is $100/10 = 10$.

OR

Regroup the fractions before adding:

$$\left(\frac{1}{10} + \frac{9}{10}\right) + \left(\frac{2}{10} + \frac{8}{10}\right) + \left(\frac{3}{10} + \frac{7}{10}\right) + \left(\frac{4}{10} + \frac{6}{10}\right) + \left(\frac{5}{10} + \frac{55}{10}\right) =$$

$$1 + 1 + 1 + 1 + 6 = 10.$$

5 / 8

$$3, \quad 2(81 + 83 + 85 + 87 + 89 + 91 + 93 + 95 + 97 + 99) =$$

- A) 1600 B) 1650 C) 1700 D) 1750 E) 1800

1987 Q3

3. E Pairing the addends as shown, we see the desired product is $(2)(5)(180) = 1800$.

$$2(81 + 83 + 85 + 87 + 89 + 91 + 93 + 95 + 97 + 99)$$

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2013 Q3

3. What is the value of $4 \cdot (-1 + 2 - 3 + 4 - 5 + 6 - 7 + \dots + 1000)$?

- (A) -10 (B) 0 (C) 1 (D) 500 (E) 2000

3. **Answer (E):** Inside the parentheses are 500 pairs of numbers, each with a sum of 1. Therefore the expression equals $4 \cdot 500 = 2000$.

7 / 8

$$4. \quad \frac{2 + 4 + 6 + \dots + 34}{3 + 6 + 9 + \dots + 51} =$$

- (A) $\frac{1}{3}$ (B) $\frac{2}{3}$ (C) $\frac{3}{2}$ (D) $\frac{17}{3}$ (E) $\frac{34}{3}$

1996 Q4

$$4. \text{ (B)} \quad \frac{2 + 4 + 6 + \cdots + 34}{3 + 6 + 9 + \cdots + 51} = \frac{2(1 + 2 + 3 + \cdots + 17)}{3(1 + 2 + 3 + \cdots + 17)} = \frac{2}{3}.$$

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1991 Q4

4. If $991 + 993 + 995 + 997 + 999 = 5000 - N$, then $N =$
(A) 5 (B) 10 (C) 15 (D) 20 (E) 25

4. (E) Each of the five numbers on the left side of the equation is approximately equal to 1,000. Thus N can be found by computing the difference between 1,000 and each number, so $N = 9 + 7 + 5 + 3 + 1 = 25$.

OR

$$\begin{aligned} \text{Since} \quad & 991 + 993 + 995 + 997 + 999 \\ &= (1000-9) + (1000-7) + (1000-5) + (1000-3) + (1000-1) \\ &= 5000 - (9 + 7 + 5 + 3 + 1) = 5000 - 25, \end{aligned}$$

it follows that $N = 25$.