18. 11-15 NUMBER Fractions ANSWERS www.AMC8prep.com

11. The sum $2\frac{1}{7} + 3\frac{1}{2} + 5\frac{1}{19}$ is between

- A) 10 and $10\frac{1}{2}$ B) $10\frac{1}{2}$ and 11 C) 11 and $11\frac{1}{2}$
- D) $11\frac{1}{2}$ and 12 E) 12 and $12\frac{1}{2}$

1987 Q11

The desired sum can be rewritten as $2 + 3 + 5 + \frac{1}{7} + \frac{1}{2} + \frac{1}{19}$ 11. which equals $10 + \frac{1}{2} + \left(a \text{ number less than } \frac{1}{2} \right)$ so B is correct.

2/12

1996 Q11

11. Let x be the number

where there are 1996 zeros after the decimal point. Which of the following expressions represents the largest number?

- (A) 3 + x
- **(B)** 3 x
- (C) $3 \cdot x$ (D) 3/x (E) x/3

11. (D) Since x is near zero, 3+x and 3-x are near 3. Also $3 \cdot x$ and x/3are near zero. However, 3/x is the number

which is a 3 followed by 1997 zeros. This number is much larger than any of the other alternatives.

3 / 12

1989 Q12

$$12. \quad \frac{1 - \frac{1}{3}}{1 - \frac{1}{2}} \quad = \quad$$

- A) $\frac{1}{3}$ B) $\frac{2}{3}$ C) $\frac{3}{4}$ D) $\frac{3}{2}$ E) $\frac{4}{3}$

12. E
$$\frac{1-\frac{1}{3}}{1-\frac{1}{2}} = \frac{\frac{2}{3}}{\frac{1}{2}} = \frac{2}{3} \times \frac{2}{1} = \frac{4}{3}$$
.

OR

Multiplying both numerator and denominator by 6 yields

$$\frac{6(1-\frac{1}{3})}{6(1-\frac{1}{2})} = \frac{6-2}{6-3} = \frac{4}{3}.$$

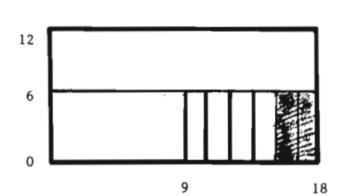
4/12

1987 Q12

12. What fraction of the large 12 by 18 rectangular region is shaded?



- D) $\frac{2}{9}$ E) $\frac{1}{3}$



The large rectangular region can be subdivided into 24 12. congruent rectangular regions of which 2 are shaded.

OR

 $\frac{1}{3}$ of $\frac{1}{4} = \frac{1}{12}$ of the rectangular region is shaded.

5 / 12

1998 Q12

- 12. $2(1-\frac{1}{2})+3(1-\frac{1}{3})+4(1-\frac{1}{4})+\ldots+10(1-\frac{1}{10})=$ (A) 45 (B) 49 (C) 50 (D) 54 (E) 55
- 12. **Answer** (**A**):

$$2(1 - \frac{1}{2}) + 3(1 - \frac{1}{3}) + 4(1 - \frac{1}{4}) + \dots + 10(1 - \frac{1}{10}) =$$

$$2(\frac{1}{2}) + 3(\frac{2}{3}) + 4(\frac{3}{4}) + \dots + 10(\frac{9}{10}) =$$

$$1 + 2 + 3 + \dots + 9 = 45.$$

6 / 12

2016 Q12

- 12. Jefferson Middle School has the same number of boys and girls. Threefourths of the girls and two-thirds of the boys went on a field trip. What fraction of the students on the field trip were girls?
- (A) $\frac{1}{2}$ (B) $\frac{9}{17}$ (C) $\frac{7}{13}$ (D) $\frac{2}{3}$ (E) $\frac{14}{15}$

12. Answer (B):

Converting the given fractions to the same denominator, we see that $\frac{9}{12}$ of the girls and $\frac{8}{12}$ of the boys went on the trip. So the ratio of the number of girls to the number of boys was 9: 8, and it follows that $\frac{9}{17}$ of the students on the trip were girls.

OR

The number of boys and girls must be a common multiple of 4 and 3, the denominators of the fractions given in the problem. Suppose there are 12 boys and 12 girls in Jefferson Middle School. Then 9 girls and 8 boys went on the trip, for a total of 17 students. The fraction of girls on the trip is 9/17.

7 / 12

13. Which of the following fractions has the largest value?

- A) $\frac{3}{7}$ B) $\frac{4}{9}$ C) $\frac{17}{35}$ D) $\frac{100}{201}$ E) $\frac{151}{301}$

1987 Q13

If the numerator of a fraction is less than half its 13. denominator, then the value of the fraction is less than $\frac{1}{2}$. Consequently all the fractions other than (E) are less than $\frac{1}{2}$ while $\frac{151}{301} > \frac{1}{2}$.

8 / 12

1989 Q13

13.
$$\frac{9}{7 \times 53} =$$

- A) $\frac{.9}{.7 \times 53}$ B) $\frac{.9}{.7 \times 53}$ C) $\frac{.9}{.7 \times 53}$ D) $\frac{.9}{.7 \times .53}$ E) $\frac{.09}{.07 \times .53}$
- To get .9 in the numerator, we must divide it by 10. To maintain equality, we 13. must also divide the denominator by 10. Thus

$$\frac{\frac{9}{10}}{\frac{7 \times 53}{10}} = \frac{\frac{9}{10}}{\frac{7}{10} \times 53} = \frac{.9}{.7 \times 53}.$$

In all other cases, the resulting fraction is $\frac{1}{10}$ or $\frac{1}{100}$ of the original fraction.

9/12

1994 Q13

- 13. The number halfway between $\frac{1}{6}$ and $\frac{1}{4}$ is

- (A) $\frac{1}{10}$ (B) $\frac{1}{5}$ (C) $\frac{5}{24}$ (D) $\frac{7}{24}$ (E) $\frac{5}{12}$

13. (C) Since $\frac{1}{6} = \frac{2}{12} = \frac{4}{24}$ and $\frac{1}{4} = \frac{3}{12} = \frac{6}{24}$, it follows that the number halfway between $\frac{1}{6}$ and $\frac{1}{4}$ is $\frac{5}{24}$.

OR

The number halfway between any two numbers is their arithmetic mean (average):

$$\frac{\frac{1}{6} + \frac{1}{4}}{2} = \frac{\frac{4+6}{24}}{2} = \frac{\frac{10}{24}}{2} = \frac{5}{24}.$$

OR

Estimating each fraction to three decimal places and calculating the average yields

$$\frac{\frac{1}{6} + \frac{1}{4}}{2} \approx \frac{0.167 + 0.250}{2} = \frac{0.417}{2} = 0.2085$$

which is closest to $\frac{5}{24} \approx 0.2083$.

10 / 12

1992 Q14

- 14. When four gallons are added to a tank that is one-third full, the tank is then one-half full. The capacity of the tank in gallons is
 - (A) 8
- (B) 12
- (C) 20
- (D) 24
- **(E)** 48
- 14. (D) Since 4 gallons is the difference between being 1/3 full and 1/2 full, it follows that 4 gallons is $\frac{1}{2} \frac{1}{3} = \frac{1}{6}$ of the capacity of the tank. Thus the capacity of the tank must be 24 gallons.

11 / 12

- 15. The reciprocal of $(\frac{1}{2} + \frac{1}{3})$ is

- A) $\frac{1}{6}$ B) $\frac{2}{5}$ C) $\frac{6}{5}$ D) $\frac{5}{2}$
 - E) 5

1988 Q15

C $\frac{1}{2} + \frac{1}{3} = \frac{5}{6}$ and its reciprocal is $\frac{6}{5}$. 15.

12 / 12

1995 Q15

- 15. What is the 100th digit to the right of the decimal point in the decimal form of 4/37?

 - (A) 0 (B) 1 (C) 2 (D) 7 (E) 8